

BIOHECHANICA - HUL Locomotorisch Stelsel

Oefeningen p 3

1. • m hand = $\frac{1,70}{2} \cdot 0,75 = 0,64 \text{ kg}$
 m voorarm = $\frac{4,2}{2} \cdot 0,75 = 1,58 \text{ kg}$
 m bovenarm = $\frac{6,6}{2} \cdot 0,75 = 2,48 \text{ kg}$
 • afstanden in newton. 1,80 m : a) X - coördinaat
 schouder - MC bovenarm = $(81,16 - 71,74) \cdot 1,80 = 16,956 \text{ cm}$
 schouder - elleboog = $(81,16 - 62,20) \cdot 1,80 = 34,128 \text{ cm}$

b) Y - coördinaat

elleboog - MC onderarm = $(62,20 - 55,33) \cdot 1,80 = 12,366 \text{ cm}$
 elleboog - MC hand = $(62,20 - 43,13) \cdot 1,80 = 34,326 \text{ cm}$

$$X_{MC} = \frac{0,64 \cdot 34,128 + 1,58 \cdot 34,128 + 2,48 \cdot 16,956}{0,64 + 1,58 + 2,48} = 25,07$$

$$Y_{MC} = \frac{0,64 \cdot 34,326 + 1,58 \cdot 12,366 + 2,48 \cdot 0}{0,64 + 1,58 + 2,48} = 8,83$$

$$2. \quad X_z = \frac{10 \cdot 4 + 40 \cdot 3 + 80 \cdot 0,5}{7,5} = 26,67$$

$$Y_z = \frac{60 \cdot 4 + 10 \cdot 3 + 20 \cdot 0,5}{7,5} = 37,33$$

$$3. \quad X_z = \frac{Z_1 \cdot X_{z1} + 2(Z_2 \cdot X_{z2} + Z_3 \cdot X_{z3} + Z_4 \cdot X_{z4}) + Z_5 \cdot X_{z5} + 2(Z_6 \cdot X_{z6} + Z_7 \cdot X_{z7} + Z_8 \cdot X_{z8})}{Z_1 + 2(Z_2 + Z_3 + Z_4) + 2(Z_6 + Z_7 + Z_8)}$$

= 34,59

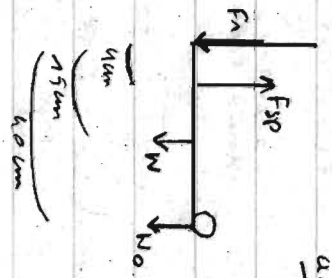
$Y_z = 56,35$

Oefeningen p 20

a & b) $\sum \vec{F}_i = 0 \quad + 0,04 \cdot F_{sp} - 0,45 \cdot 20 - 0,40 \cdot 49,05 = 0$

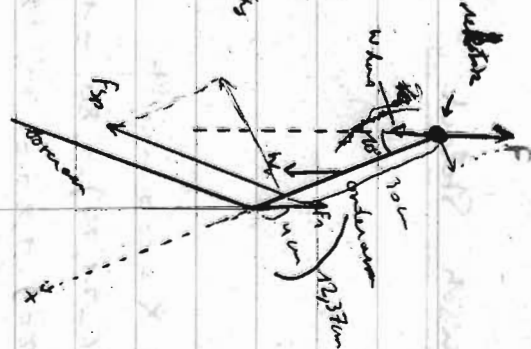
$F_{sp} = 565,5$

de kracht maakt met uit



2) Wahsen

Zuehndat pt
 $W_h = 1,58 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}}$
 $= 15,50 \text{ N}$
 $W_h = 0,64 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}}$
 $= 6,29 \text{ N}$



$F = 76 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} = 735,76 \text{ N}$

$\sum \vec{F}_x = 0 \Rightarrow + W_h \cdot 0,34 \cdot \sin 10^\circ + W \cdot \sin 10^\circ - 0,1933$
 $\downarrow - \frac{F}{2} \cdot 0,34 \cdot \sin 10^\circ + F_{sp} \cdot 0,04 \cdot \sin 20^\circ = 0$

\Rightarrow per wasser $F_{sp} = 1636,11 \text{ N}$

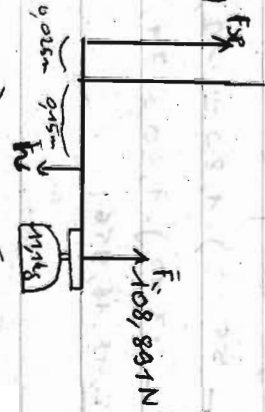
~~$F_{sp} = F$~~ $F_x: F_{sp} \cdot \cos 10^\circ + W_h \cdot \cos 10^\circ + W \cdot \cos 10^\circ + F_{sp} \cdot \cos 20^\circ$

~~$F = 3202,18 \text{ N}$~~ $F_{sp} = 7305,75 \text{ N} = 8439,43 \text{ N}$

~~$F_{y1}: F_{sp} + F_h \cdot \sin 10^\circ + W_h \cdot \sin 10^\circ + F_{sp} \cdot \sin 20^\circ = 0$~~
 ~~$F_{y2}: F_{sp} + 465,28$~~

$\Rightarrow F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2} = 1196,79$

3) Fsp



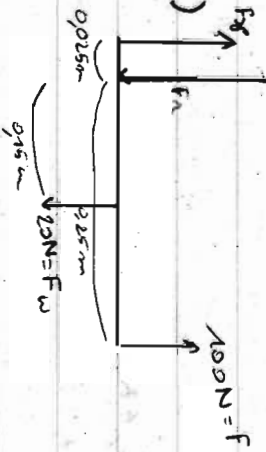
$F = 11,1 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}}$

$W = 2,2 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} = 21,582 \text{ N}$

$\sum \vec{T}_G = 0 \Rightarrow -F_{sp} \cdot 0,025 - 21,582 \cdot 0,150 + 108,891 \cdot 0,33 = 0$

$\Rightarrow F_{sp} = 1177,2$

4) Fh



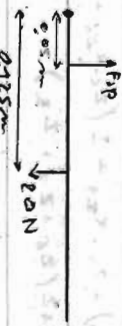
$\sum \vec{T}_G = 0 \Rightarrow -F_{sp} \cdot 0,025 - 20 \cdot 0,15 + 100 \cdot 0,25 = 0$

$F_{sp} = 880 \text{ N}$

$-F_A + F_{sp} - F_N + F = 0$

$F_A = 960 \text{ N}$

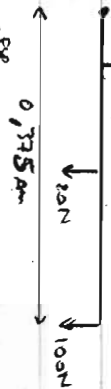
5) a) Fsp



$\sum \vec{T}_G = 0 \Rightarrow 0,05 \cdot F_{sp} - 0,125 \cdot 20 = 0$

$\Rightarrow F_{sp} = 50 \text{ N} \rightarrow$ Abstand 50N senkrecht

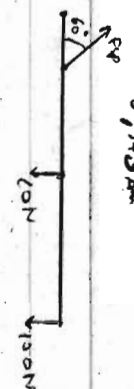
b) Fsp



$\sum \vec{T}_G = 0 \Rightarrow 0,05 \cdot F_{sp} - 0,125 \cdot 20 - 0,375 \cdot 100 = 0$

$\Rightarrow F_{sp} = 800 \text{ N}$ - Abstand

c) Fsp



$\sum \vec{T}_G = 0 \Rightarrow 1 \cdot 0,05 \cdot F_{sp} \cdot \sin 60^\circ - 0,125 \cdot 20 - 0,375 \cdot 100 = 0$

$\Rightarrow F_{sp} = 324 \text{ N}$ - Abstand: 462 N

$F_{y1} = -800 + 20 + 100 = -680 \text{ N}$, $F_{Ax} = 462 \text{ N} \Rightarrow F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2} = 822 \text{ N}$

$\sum \vec{T}_G = 0 \Rightarrow F_{sp} \cdot 0,05 \cdot \sin 15^\circ - 0,125 \cdot 20 - 0,375 \cdot 100 = 0$

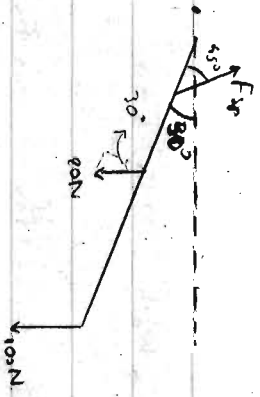
$\Rightarrow F_{sp} = 3041 \text{ N}$ - Abstand: 800 N

$F_{Ay} = -800 + 20 + 100 = -680 \text{ N}$, $F_{Ax} = 2916 \text{ N} \Rightarrow F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2} = 3062$

$\sum \vec{T}_G = 0 \Rightarrow 0,05 \cdot \sin 45^\circ \cdot F_{sp} - 0,125 \cdot 20 - 0,375 \cdot 100 = 0$

$\Rightarrow F_{sp} = 980 \text{ N}$ - Abstand: 693 N

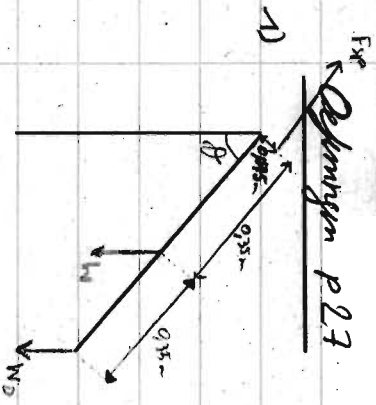
$\Rightarrow F_{sp} = 980 \text{ N}$ - Abstand: 693 N



d) hoch gerechnet, geht gleichwohl 777

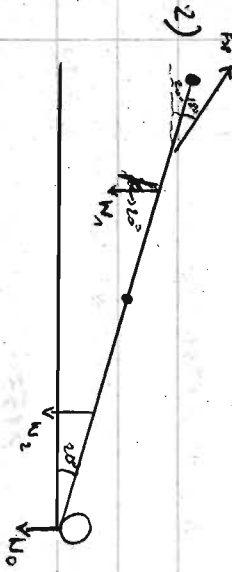
$$\begin{aligned} \sum \vec{T}_0 = 0 &\Rightarrow +0,05 \cdot m \cdot 45^\circ \cdot F_{sp} - 0,125 \cdot 200 \cdot \cos 30^\circ - 0,375 \cdot 100 \cdot \cos 30^\circ = 0 \\ &\Rightarrow F_{sp} = 980 \text{ N} \quad \text{Antwort A: } 693 \text{ N} \\ &\quad \text{Problem 1: } 693 \text{ N} \\ F_{ry} &= -693 + \cos 30^\circ \cdot 20 + \cos 30^\circ \cdot 100 = -583 \\ F_{rx} &= -693 + \sin 30^\circ \cdot 20 + \sin 30^\circ \cdot 100 = -633 \end{aligned}$$

1) Rechnung p 23



$$\Rightarrow F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2} = 1064 \text{ N}$$

$$\begin{aligned} W_0 &= 9 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} = 88 \text{ N} \\ W &= \frac{6,5}{100} \cdot 79 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} = 50 \text{ N} \\ \sum \vec{T}_0 = 0 &\Rightarrow 0,035 \cdot F_{sp} - W \cdot \sin \theta \cdot 0,35 - W_0 \cdot \sin \theta \cdot 0,70 = 0 \\ &\Rightarrow F_{sp} = 1055 \text{ N} \cdot \sin \theta \\ \sum F_x = 0 &\Rightarrow F_{Ax} - F_{sp} = 0 \Rightarrow F_{Ax} = 1055 \text{ N} \cdot \sin 30^\circ \\ \sum F_y = 0 &\Rightarrow F_{Ay} - \sin \theta \cdot W - W_0 \cdot \sin \theta = 138 \text{ N} \end{aligned}$$



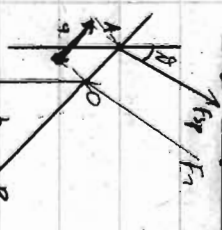
$$\begin{aligned} \sum \vec{T}_0 = F_{sp} \cdot \sin 18^\circ \cdot 0,16 - W_1 \cdot 0,16 - W_2 \cdot 0,56 - W_0 \cdot 0,70 &= 0 \\ \Rightarrow F_{sp} = 861,54 \text{ N} \\ \sum F_x = F_{Ax} - F_{sp} \cdot \cos 38^\circ = 0 &\Rightarrow F_{Ax} = 678,90 \text{ N} \\ \sum F_y = F_{Ay} + \sin 38^\circ \cdot F_{sp} - W_1 - W_2 - W_0 = 0 &\Rightarrow F_{Ay} = -442,10 \end{aligned}$$



$$\begin{aligned} \Rightarrow \theta = 20^\circ = \text{hoch mit Formeln} &= 13,07^\circ \\ W &= 3,3 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} = 32,372 \text{ N} \\ F_y &= 65 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} = 637,35 \text{ N} \\ \sum \vec{T}_0 = -F_{sp} \cdot \sin 30^\circ \cdot 0,07 - W \cdot 0,25 + F_y \cdot 0,60 = 0 &\Rightarrow F_{sp} = 5234 \text{ N} \\ \sum F_x = -F_{sp} \cdot \cos 30^\circ + F_{Ax} - F \cdot \cos 78^\circ = 0 &\Rightarrow F_{Ax} = 4598 \text{ N} \\ \sum F_y = -F_{sp} \cdot \sin 30^\circ + F_{Ay} - W + F \cdot \sin 78^\circ = 0 &\Rightarrow F_{Ay} = 2344,33 \text{ N} \\ \Rightarrow F_A = 5161 \text{ N} & \quad \theta = 27^\circ \end{aligned}$$

Dejavnost P 38

1)



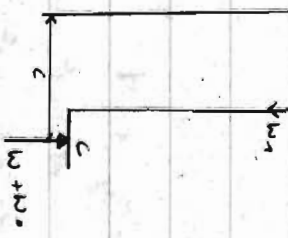
$$\sum \vec{T}_0 = + F_{sp} \cos \beta \cdot a - W_1 \cdot b + (W_1 + W_2) \cdot c = 0$$

$$F_{sp} = 14,7 \text{ kN}$$

$$\sum F_y = F_{sp} \cos \beta - W_1 + W_1 + W_2 + F_{xy} = 0 \Rightarrow F_{xy} = -12 \text{ kN}$$

$$\sum F_x = F_{sp} \sin \beta + F_{xx} = 0 \Rightarrow F_{xx} = -10 \text{ kN}$$

$$\Rightarrow F_n = \sqrt{F_{xx}^2 + F_{xy}^2} = 15,6 \text{ kN}$$



2)

$$\sum \vec{T}_1 = 0 \Rightarrow + F_{sp} \sin 12^\circ \cdot 0,7 - W \cdot 0,6 - W_1 \cdot 1 = 0 \Rightarrow F_{sp} = 2020 \text{ N}$$

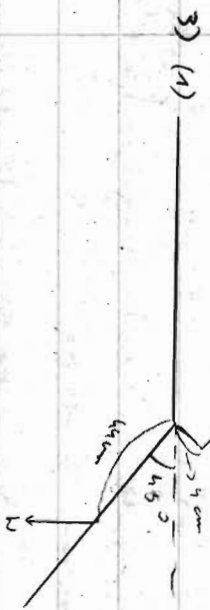
$$\sum F_x = - \cos 12^\circ \cdot F_{sp} + F_{xx} = 0 \Rightarrow F_{xx} = 1976 \text{ N}$$

$$\sum F_y = \sin 12^\circ \cdot F_{sp} - W + F_{yy} = 0 \Rightarrow F_{yy} = 70 \text{ N}$$

$$\sum \vec{T}_2 = 0 \Rightarrow + F_{sp} \sin 12^\circ \cdot 0,7 - W \cdot 0,6 - W_1 \cdot 1 = 0 \Rightarrow F_{sp} = 3223 \text{ N}$$

$$\sum F_x = - \cos 12^\circ \cdot F_{sp} + F_{xx} = 0 \Rightarrow F_{xx} = 3153 \text{ N}$$

$$\sum F_y = + \sin 12^\circ \cdot F_{sp} - W - W_1 + F_{yy} = 0 \Rightarrow F_{yy} = -5 \text{ N}$$



$$W = 37 \text{ kg} \cdot 9,81 \frac{\text{m}}{\text{s}^2} = 363 \text{ N}$$

$$\sum \vec{T}_0 = 0 \Rightarrow F_{sp} \cdot 0,4 - W \cdot 0,4 \cdot \sin 45^\circ = 0$$

$$\Rightarrow F_{sp} = 2823$$



$$\sum \vec{T}_0 = 0 \Rightarrow F_{sp} \cdot 0,4 - W \cdot 0,4 = 0$$

$$\Rightarrow F_{sp} = 3993$$



$$\sum \vec{T}_0 = 0 \Rightarrow F_{sp} \cdot 0,4 - W \cdot \cos 35^\circ \cdot 0,4 = 0$$

$$\Rightarrow F_{sp} = 2823$$

Deleming p 50

1. a) $\sum F_x = 0$ $-W \cdot x + \frac{W}{2} (0,30 + x) = 0$

$\Rightarrow -x + \frac{0,30}{2} + \frac{x}{2} = 0$

$\Rightarrow \frac{5x}{2} = \frac{-0,30}{2}$

$\Rightarrow x = 0,06 \text{ m}$ \downarrow 6 cm

b) $\sum T_i = 0$ $-N \cdot 0,05 - W_{\text{lem}} \cdot 0,03 + \sin 31^\circ \cdot F_{sp} \cdot 0,07 = 0$

$\Rightarrow F_{sp} = 622,8 \text{ N}$

$\sum F_y = 0$ $\Rightarrow 2F_{sp} \cdot \sin 31^\circ - W_{\text{lem}} + N + F_{Ay} = 0$ $\Rightarrow F_{Ay} = -1192,5 \text{ N}$

$\sum F_x = 0$ $\Rightarrow \cos 31^\circ \cdot F_{sp} + F_{Ax} = 0$ $\Rightarrow F_{Ax} = -202,76 \text{ N}$

$\Rightarrow F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2} = \boxed{1210 \text{ N}}$

2. $\sum \tau (\text{sum}) = 0$ $-W \cdot 0,12 + F_{sp} \cdot 0,1 = 0$ $\Rightarrow F_{sp} = 1283 \text{ N}$

$\sum T (\text{sum}) = 0$ $-F_{sp} \cdot 0,07 + F \cdot 0,35 = 0$ $\Rightarrow \boxed{F = 258 \text{ N}}$

Deleming p 64

1. a). berp F_1 : $\sum T_i = 0 \Rightarrow +F_1 \cdot \frac{I_A}{\cos 30^\circ} - F_m \cdot 1,30 = 0$

$\Rightarrow F_1 = 57,5 \text{ N}$

berp F_{sp} :

$\sum T_i = 0 \Rightarrow +F_{sp} \cdot 0,05 - N_b \cdot 0,20 - F_1 (I_A - I_k) = 0$

$\Rightarrow F_{sp} = 307 \text{ N}$

b). berp F_2 :

$\sum T_i = 0 \Rightarrow +F_2 \cdot \frac{I_B}{\cos 30^\circ} - F_m \cdot 1,30 = 0$

$\Rightarrow F_2 = 28 \text{ N}$

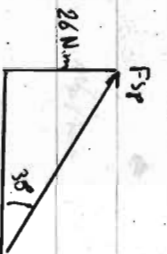
berp F_{sp} : $\sum T_i = 0 \Rightarrow +F_{sp} \cdot 0,05 - N_b \cdot \sin 46^\circ \cdot 0,20 - F_2 (I_A - I_k) \cdot \sin 45^\circ = 0$

$\Rightarrow F_{sp} = 647 \text{ N}$

2.



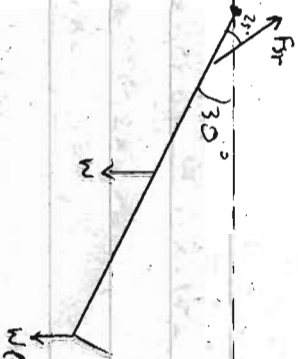
$\sum T_i = 0 \Rightarrow 26 \text{ N} \cdot \text{m} - 50 \text{ N} \cdot 0,12 \text{ m} + F_1 \cdot 0,335 = 0$ $\Rightarrow F_1 = -53,3 \text{ N}$



$\Rightarrow \frac{26 \text{ N} \cdot \text{m}}{0,05 \text{ m}} = 520 \text{ N}$

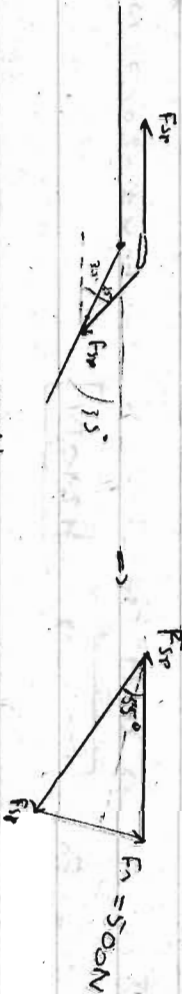
$\frac{520 \text{ N}}{\sin 38^\circ} = F_{sp} = 1040$

3.



$$\sum T_i = 0 \Rightarrow F_{SP} \cdot \sin 25^\circ \cdot 0,05 - W \cdot \sin 60^\circ \cdot 0,25 - F_L \cdot \sin 60^\circ \cdot 0,33 = 0$$

$$F_{SP} = \frac{W \cdot \sin 60^\circ \cdot 0,25 + F_L \cdot \sin 60^\circ \cdot 0,33}{\sin 25^\circ \cdot 0,05} \quad (1)$$



$$F_{SP} = \frac{250 \text{ N} \cdot \frac{300 \text{ N}}{2}}{\sin 27,5^\circ \cdot \frac{65^\circ}{2}} = 544,42 \text{ N} \quad (1) \Rightarrow F_L = 8,7 \text{ N}$$

Aufgaben p 68

1. a)



$$\sum T_i = 0 \Rightarrow -F_{SP} \cdot 0,06 + \frac{W_L}{2} \cdot 0,10 = 0 \Rightarrow F_{SP} = 619 \text{ N}$$

zur Lösung gezeichnet mit anschließender Lösung

$$a) \sum F_x = 0 \Rightarrow F_{SP} \cdot \sin 30^\circ + F_{Ax} = 0 \Rightarrow F_{Ax} = -306,5 \text{ N}$$

$$\sum F_y = 0 \Rightarrow F_{SP} \cdot \cos 30^\circ + \frac{W_L}{2} + F_{Ay} = 0 \Rightarrow F_{Ay} = -898,7 \text{ N} \quad \left. \begin{array}{l} \Rightarrow F_A = 949 \text{ N} \end{array} \right\}$$

$$c) \sum F_x = 0 \Rightarrow F_{1x} = \cos 45^\circ \cdot 991 \text{ N} - \cos 70^\circ \cdot 991 \text{ N} = 0 \Rightarrow F_{Ax} = 1010 \text{ N} \quad \left. \begin{array}{l} \Rightarrow F_A = 1065 \text{ N} \end{array} \right\}$$

$$\sum F_y = 0 \Rightarrow F_{1y} + \sin 45^\circ \cdot 991 \text{ N} - \sin 70^\circ \cdot 991 \text{ N} = 0 \Rightarrow F_{Ay} = 239,5 \text{ N}$$

$$\sum T_i = 0 \Rightarrow -2100 \cdot d_3 + 1095 \cdot d_2 + F_{SP} \cdot d_1 = 0 \Rightarrow F_{SP} = 6290 \text{ N}$$



$$\Rightarrow \textcircled{1} \text{ L.o.} \quad \sum T_i = 0 \quad T \cdot 0,105 - W_L \cdot 0,116 = 0$$

$$\Rightarrow T = 597 \text{ N}$$

$$\Rightarrow \textcircled{2} \text{ L.o.} \quad \sum T_i = 0 \quad T \cdot 0,081 + F_A \cdot 0,025 - W_L \cdot 0,116 = 0$$

$$\Rightarrow F_A = 1135 \text{ N}$$

⑥